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Exemple: 1

exprimer en fonction de  $\ln 2, \ln 3$  et  $\ln 5$

$$\bullet A = \ln\left(\sqrt{\frac{9}{25}}\right); \bullet B = \ln(3\sqrt{15});$$

$$\bullet C = \ln\left(\sqrt{\frac{1}{75}}\right);$$

$$\bullet D = \ln\frac{1}{2} + \ln\left(\frac{2}{3}\right) + \ln\left(\frac{3}{4}\right) + \dots + \ln\left(\frac{99}{100}\right)$$

$$\bullet E = \ln(1000); \bullet F = \ln(0,02).$$

Solution:

$$\bullet A = \ln\left(\sqrt{\frac{9}{25}}\right) = \ln\left(\frac{3}{5}\right)$$

$$\Rightarrow A = \ln 3 - \ln 5$$

$$\begin{aligned} \bullet B &= \ln(3\sqrt{15}) = \ln 3 + \ln \sqrt{15} \\ &= \ln 3 + \frac{1}{2}(\ln 3 + \ln 5) \\ &= \ln 3 + \frac{1}{2}\ln 3 + \frac{1}{2}\ln 5 \end{aligned}$$

$$B = \frac{3}{2}\ln 3 + \frac{1}{2}\ln 5$$

$$\begin{aligned} \bullet C &= \ln\left(\sqrt{\frac{1}{75}}\right) = +\frac{1}{2}\left(\frac{1}{75}\right) \\ &= -\frac{1}{2}\ln(75) = -\frac{1}{2}\ln(25 \times 3) \\ &= -\frac{1}{2}(\ln 25 + \ln 3) = -\frac{1}{2}(\ln 5^2 + \ln 3) \end{aligned}$$

$$\Rightarrow C = -\ln 5 - \frac{1}{2}\ln 3$$

$$\bullet D = \ln\frac{1}{2} + \ln\left(\frac{2}{3}\right) + \ln\left(\frac{3}{4}\right) + \dots + \ln\left(\frac{99}{100}\right)$$

(M<sub>1</sub>):

$$\begin{aligned} D &= \ln 1 - \ln 2 + \ln 2 - \ln 3 + \ln 3 - \ln 4 + \dots \\ &\quad + \ln 99 - \ln 100 = -\ln 100 \\ &= -\ln 10^2 = -2\ln 10 \\ &= -2\ln(5 \times 2) = -2(\ln 5 + \ln 2) \end{aligned}$$

$$\Rightarrow D = -2\ln 5 - 2\ln 2$$

(M<sub>2</sub>)

$$D = \ln\left[\frac{1}{2} \times \frac{2}{3} \times \frac{3}{4} \times \dots \times \frac{98}{99} - \frac{99}{100}\right]$$

$$D = -\ln 100$$

$$\begin{aligned} \bullet E &= \ln(1000) = \ln 10^3 = 3\ln 10 \\ &= 3\ln(2 \times 5) = 3(\ln 2 + \ln 5) \end{aligned}$$

$$\Rightarrow E = 3\ln 2 + 3\ln 5$$

$$\bullet F = \ln(0,02) = \ln(2 \cdot 10^{-2})$$

$$= \ln 2 + \ln 10^{-2} = \ln 2 - 2\ln 2 - 2\ln 5$$

$$F = -\ln 2 - 2\ln 5$$

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